

# **Dimensional Analysis and Metric Conversions**



# SC Standards

## PS-1.5

Organize and interpret the data from a controlled scientific investigation by using mathematics (including formulas and dimensional analysis), graphs, models, and/or technology.



# Dimensional Analysis

## Conversion factors:


- using ratios of equivalent values to convert from one unit of measure to another.

$$1 \text{ gram} = 1000 \text{ milligrams}$$

$$\frac{1 \text{ g}}{1000 \text{ mg}}$$

or

$$\frac{1000 \text{ mg}}{1 \text{ g}}$$


$$60 \text{ sec} = 1 \text{ min.}$$

$$\frac{60 \text{ sec}}{1 \text{ min.}} \quad \text{or} \quad \frac{1 \text{ min.}}{60 \text{ sec}}$$

What would the conversion factors be for years and days?


$$\frac{365 \text{ days}}{1 \text{ year}} \quad \text{or} \quad \frac{1 \text{ year}}{365 \text{ days}}$$

# Dimensional Analysis


- 1.) Write down given number and unit
- 2.) Write down "x" and a line
- 3.) Put given unit on side of line so it will cancel and the desired unit on the other side (may take more than 1 step)
- 4.) Fill in appropriate numerical relationship for the ratio
- 5.) Multiply the top and divide by the bottom

...see examples...

- Example #1
  - How many minutes are there in 1 year?


$$1 \text{ year} \times \frac{365 \text{ days}}{1 \text{ year}} \times \frac{24 \text{ hr}}{1 \text{ day}} \times \frac{60 \text{ min.}}{1 \text{ hr}}$$

$$= \underline{525,600 \text{ minutes!!}}$$



Example #2 - How many inches are there in 85.6 cm? (1in = 25.4mm)

$$85.6\cancel{\text{cm}} \times \frac{10\cancel{\text{mm}}}{1\cancel{\text{cm}}} \times \frac{1\text{ in}}{25.4\cancel{\text{mm}}} = 33.7\text{ in.}$$

## Example #3 - How many fluid ounces are there in 2.0 gallons?

(1 gall = 4 qts, 1 qt = 2 pints, 1 pint = 2 cups,  
1 cup = 8 fl. oz.)

$$2.0 \text{ gall} \quad \times \frac{4 \text{ qts}}{1 \text{ gal}} \quad \times \frac{2 \text{ pt}}{1 \text{ qt.}}$$

$$\times \frac{2 \text{ cup}}{1 \text{ pt.}} \quad \times \frac{8 \text{ fl. oz.}}{1 \text{ cup}}$$

$$= 256 \text{ fl. oz.}$$

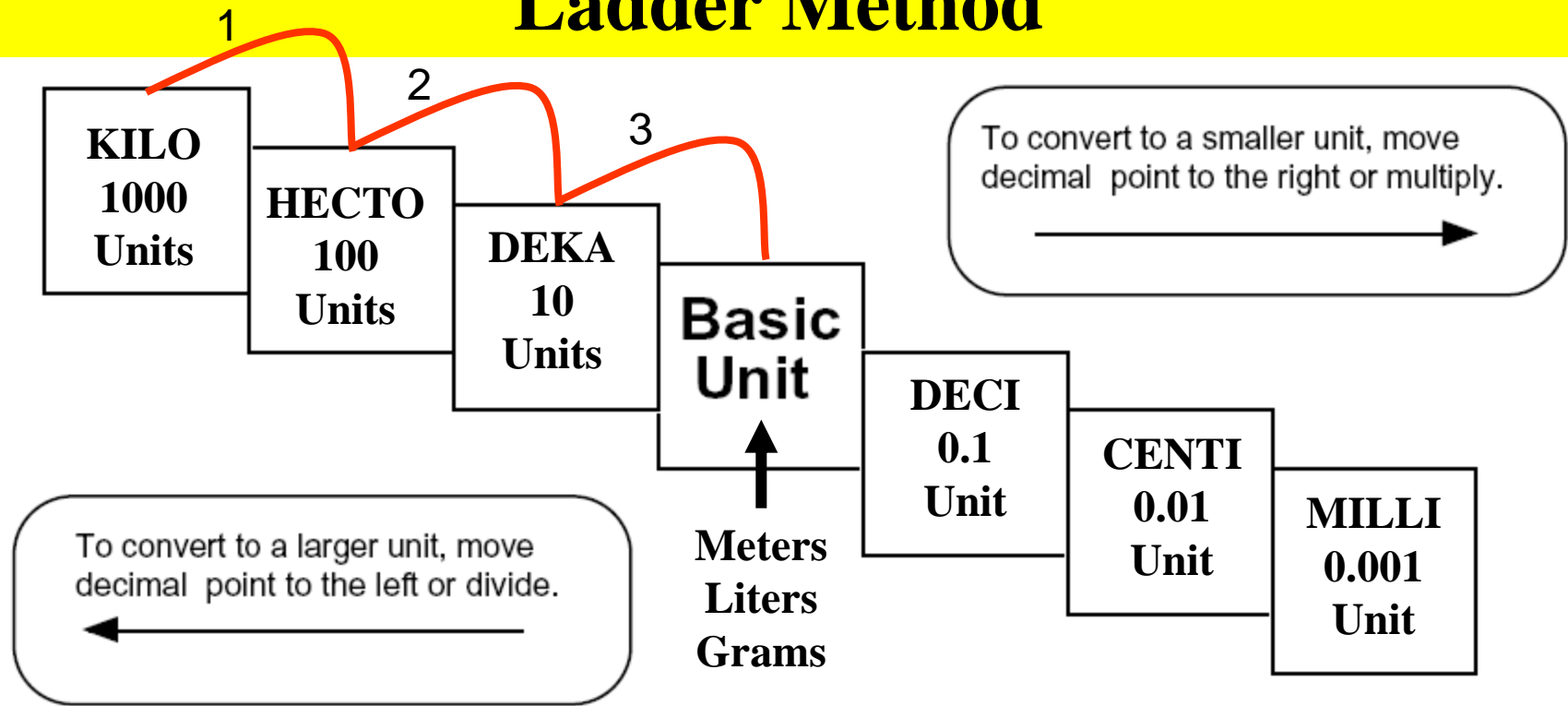


# Metric Mania



## Metric Conversions Ladder Method

# Ladder Method



## How do you use the “ladder” method?

1<sup>st</sup> – Determine your starting point.

2<sup>nd</sup> – Count the “jumps” to your ending point.

3<sup>rd</sup> – Move the decimal the same number of jumps in the same direction.

$$4 \text{ km} = \underline{\hspace{2cm}} \text{ m}$$

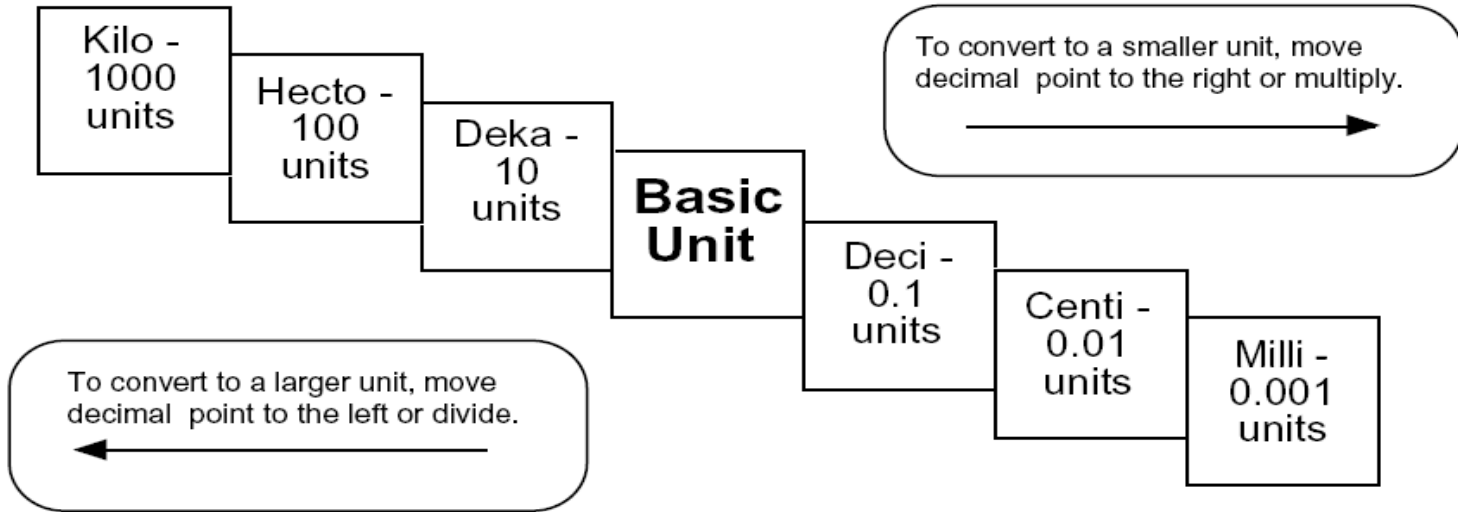
Starting Point      Ending Point

How many jumps does it take?

$$4.\underline{\hspace{0.5cm}}\underline{\hspace{0.5cm}}\underline{\hspace{0.5cm}} = 4000 \text{ m}$$

1 2 3

# Conversion Practice



Try these conversions using the ladder method.

$1000 \text{ mg} = \underline{\hspace{2cm}} \text{ g}$

$1 \text{ L} = \underline{\hspace{2cm}} \text{ mL}$

$160 \text{ cm} = \underline{\hspace{2cm}} \text{ mm}$

$14 \text{ km} = \underline{\hspace{2cm}} \text{ m}$

$109 \text{ g} = \underline{\hspace{2cm}} \text{ kg}$

$250 \text{ m} = \underline{\hspace{2cm}} \text{ km}$

Compare using  $<$ ,  $>$ , or  $=$ .

$56 \text{ cm} \bigcirc 6 \text{ m}$

$7 \text{ g} \bigcirc 698 \text{ mg}$

# Metric Conversion Challenge

**Write the correct abbreviation for each metric unit.**

1) Kilogram \_\_\_\_\_

4) Milliliter \_\_\_\_\_

7) Kilometer \_\_\_\_\_

2) Meter \_\_\_\_\_

5) Millimeter \_\_\_\_\_

8) Centimeter \_\_\_\_\_

3) Gram \_\_\_\_\_

6) Liter \_\_\_\_\_

9) Milligram \_\_\_\_\_

**Try these conversions, using the ladder method.**

10) 2000 mg = \_\_\_\_\_ g

15) 5 L = \_\_\_\_\_ mL

20) 16 cm = \_\_\_\_\_ mm

11) 104 km = \_\_\_\_\_ m

16) 198 g = \_\_\_\_\_ kg

21) 2500 m = \_\_\_\_\_ km

12) 480 cm = \_\_\_\_\_ m

17) 75 mL = \_\_\_\_\_ L

22) 65 g = \_\_\_\_\_ mg

13) 5.6 kg = \_\_\_\_\_ g

18) 50 cm = \_\_\_\_\_ m

23) 6.3 cm = \_\_\_\_\_ mm

14) 8 mm = \_\_\_\_\_ cm

19) 5.6 m = \_\_\_\_\_ cm

24) 120 mg = \_\_\_\_\_ g

**Compare using <, >, or =.**

25) 63 cm ○ 6 m

27) 5 g ○ 508 mg

29) 1,500 mL ○ 1.5 L

26) 536 cm ○ 53.6 dm

28) 43 mg ○ 5 g

30) 3.6 m ○ 36 cm