Chapter 13

Gases



Chapter Map







Gas Model

- Gases are composed of tiny, widely-spaced particles.
 - For a typical gas, the average distance between particles is about ten times their diameter.



- Because of the large distance between the particles, the volume occupied by the particles themselves is negligible (approximately zero).
 - For a typical gas at room temperature and pressure, the gas particles themselves occupy about 0.1% of the total volume. The other 99.9% of the total volume is empty space. This is very different than for a liquid for which about 70% of the volume is occupied by particles.

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- The particles have rapid and continuous motion.
 - For example, the average velocity of a helium atom, He, at room temperature is over 1000 m/s (or over 2000 mi/hr). The average velocity of the more massive nitrogen molecules, N₂, at room temperature is about 500 m/s.
 - Increased temperature means increased average velocity of the particles.

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- The particles are constantly colliding with the walls of the container and with each other.
 - Because of these collisions, the gas particles are constantly changing their direction of motion and their velocity. In a typical situation, a gas particle moves a very short distance between collisions.
 Oxygen, O₂, molecules at normal temperatures and pressures move an average of 10⁻⁷ m between collisions.

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 There is no net loss of energy in the collisions. A collision between two particles may lead to each particle changing its velocity and thus its energy, but the increase in energy by one particle is balanced by an equal decrease in energy by the other particle.

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Ideal Gas

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- The particles are assumed to be point-masses, that is, particles that have a mass but occupy no volume.
- There are no attractive or repulsive forces at all between the particles.

Gas Properties and their Units

• Pressure (P) = Force/Area

units

- 1 atm = 101.325 kPa = 760 mmHg = 760 torr
- 1 bar = 100 kPa = 0.9869 atm = 750.1 mmHg
- Volume (V)

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- unit usually liters (L)
- Temperature (T)
 -? K = --- °C + 273.15
- Number of gas particles expressed in moles (n)

Gas Law Objectives

- For each of the following pairs of gas properties, (1) describe the relationship between them, (2) describe a simple system that could be used to demonstrate the relationship, and (3) explain the reason for the relationship.
 - V and P when n and T are constant
 - P and T when n and V are constant
 - V and T when n and P are constant

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- n and P when V and T are constant
- n and V when P and T are constant

Apparatus for Demonstrating Relationships Between Properties of Gases



Decreased Volume Leads to Increased Pressure



$P \alpha 1/V$ if n and T are constant



Boyle's Law

• The pressure of an ideal gas is inversely proportional to the volume it occupies if the moles of gas and the temperature are constant.

Boyle's Law
$$P \propto \frac{1}{V}$$
 if n and T are constant

Decreased volume \rightarrow Increased pressure Increased volume \rightarrow Decreased pressure

Increased Temperature Leads to Increased Pressure



 $P \alpha T$ if n and V are constant



Gay-Lussac's Law

• The pressure of an ideal gas is directly proportional to the Kelvin temperature of the gas if the volume and moles of gas are constant.

$P \propto T$ if n and V are constant

Increased temperature \rightarrow Increased pressure Decreased temperature \rightarrow Decreased pressure

Increased Temperature Leads to Increased Volume



$V \alpha T$ if n and P are constant

Relationship between T and V



Charles' Law

• For an ideal gas, volume and temperature described in kelvins are directly proportional if moles of gas and pressure are constant.

$V \propto T$ if n and P are constant

Increased temperature → Increased volume Decreased temperature → Decreased volume

Increased Moles of Gas Leads to Increased Pressure



 $P \alpha n$ if T and V are constant

Relationship between n and P

Increased number of gas particles

Increased number of collisions with the walls Increased total force of collisions Increased gas pressure

Relationship Between Moles of Gas and Pressure

• If the temperature and the volume of an ideal gas are held constant, the moles of gas in a container and the gas pressure are directly proportional.

 $P \propto n$ if T and V are constant Increased moles of gas \rightarrow Increased pressure Decreased moles of gas \rightarrow Decreased pressure

Increased Moles of Gas Leads to Increased Volume



$V \alpha n$ if T and P are constant

Relationship between n and V



Avogadro's Law

• For an ideal gas, the volume and moles of gas are directly proportional if the temperature and pressure are constant.

$V \propto n$ if T and P are constant

Increased moles of gas \longrightarrow Increased volume Decreased moles of gas \longrightarrow Decreased volume





101.3 kPa

101.7 kPa

Breathing

Ideal Gas Equation

 $P \propto n$ if T and V are constant $P \propto T$ if *n* and *V* are constant or $P \propto \frac{nT}{V}$ $P \propto \frac{1}{V}$ if *n* and *T* are constant so $P = (a \text{ constant}) \frac{nT}{V}$ $PV = nRT \quad \frac{0.082058 \text{ L} \cdot \text{atm}}{\text{K} \cdot \text{mol}} \quad \text{or} \quad \frac{8.3145 \text{ L} \cdot \text{kPa}}{\text{K} \cdot \text{mol}}$

Ideal Gas Equation Problems

 Tip-off – The usual tip-off that you can use the ideal gas equation to answer a question is that you are given three properties of a sample of gas and asked to calculate the fourth. A more general tip-off is that only one gas is mentioned and there are no changing properties.

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Ideal Gas Equation Problem Step 1

 Step 1: Assign variables to the values given and the value that is unknown. Use P for pressure, V for volume, n for moles, T for temperature, g for mass, and M for molar mass.

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Ideal Gas Equation Problem Step 2

- Step 2: Write the appropriate form of the Ideal Gas Equation.
 - If the number of particles is given or desired in moles, use the most common form of the ideal gas equation.
 - If mass or molar mass is given or desired, use the expanded form of the ideal gas equation.

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$$PV = nRT$$
 $PV = \frac{g}{M}RT$

Ideal Gas Equation Problem Steps 3-6

- Step 3: Rearrange the equation to isolate the unknown.
- Step 4: Plug in the known values, including units. Be sure to use kelvin temperatures.
- Step 5: Make any necessary unit conversions and cancel your units.

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• Step 6: Calculate your answer and report it to the correct significant figures and with the correct unit.

 $\frac{PV}{nT} = R$ $\frac{P_1V_1}{n_1T_1} = R$ $P_1V_1 = n_1RT_1$ SO $\frac{P_2 V_2}{n_2 T_2} = R$ $P_2V_2 = n_2RT_2$ SO Combined P_1V_1 P_2V_2 **Gas Law** n_2T_2 $n_1 T_1$ Equation

Combined Gas Law Equation Problems

 Tip-off – The problem requires calculating a value for a gas property that has changed. In other words, you are asked to calculate a new pressure, temperature, moles (or mass), or volume of gas given sufficient information about the initial and other final properties.

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Combined Gas Law Equation Problem Steps 1 and 2

- Step 1: Assign the variables P, T, n, and V to the values you are given and to the unknown value. Use the subscripts 1 and 2 to show initial or final conditions.
- Step 2: Write out the combined gas law equation, but eliminate the variables for any constant properties. (You can assume that the properties not mentioned in the problem remain constant.)

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Combined Gas Law Equation Problem Steps 1 and 2

- Step 3: Rearrange the equation to isolate the unknown property.
- Step 4: Plug in the values for the given properties.
- Step 5: Make any necessary unit conversions and cancel your units.

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• Step 6: Calculate your answer and report it with the correct units and significant figures.

Equation Stoichiometry



Dalton's Law of Partial Pressures



 $P_{total} = P_A + P_B$

Dalton's Law of Partial Pressures Problems

 Tip-off – The problem involves a mixture of gases and no chemical reaction. You are asked to calculate a value for one of the variables in the equations below, and you are given (directly or indirectly) values for the other variables.

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Dalton's Law of Partial Pressures Problem Steps 1 & 2

- Step 1: Assign variables to the values that are given and the value that is unknown.
- Step 2: From the following equations, choose the one that best fits the variables assigned in Step 1.

$$P_{\text{total}} = \Sigma P_{\text{partial}}$$
 or $P_{\text{total}} = (\Sigma n_{\text{each gas}}) \frac{RT}{V}$

Dalton's Law of Partial Pressures Problem Steps 3-6

- Step 3: Rearrange the equation to solve for your unknown.
- Step 4: Plug in the values for the given properties.
- Step 5: Make sure that the equation yields the correct units. Make any necessary unit conversions.
- Step 6: Calculate your answer and report it with the correct units and significant figures.

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